

Let's find $\text{gcd}(e, j) = \text{gcd}(197, 352)$ using Extended Euclid's Algorithm:

$$\text{gcd}(197, 352) =$$

$x = 197$ (divisor)
 $y = 352$ (dividend)

$d = 352 \text{ div } 197 = 1$
 $r = 352 - 1 * 197 = 155$
 $y = x = 197$
 $x = r = 155$

$$= \text{gcd}(155, 197) =$$

$d = 197 \text{ div } 155 = 1$
 $r = 197 - 1 * 155 = 42$
 $y = x = 155$
 $x = r = 42$

$$= \text{gcd}(42, 155) =$$

$d = 155 \text{ div } 42 = 3$
 $r = 155 - 3 * 42 = 29$
 $y = x = 42$
 $x = r = 29$

$$= \text{gcd}(29, 42) =$$

$d = 42 \text{ div } 29 = 1$
 $r = 42 - 1 * 29 = 13$
 $y = x = 29$
 $x = r = 13$

$$= \text{gcd}(13, 29) =$$

$d = 29 \text{ div } 13 = 2$
 $r = 29 - 2 * 13 = 3$
 $y = x = 13$
 $x = r = 3$

$$= \text{gcd}(3, 13) =$$

$d = 13 \text{ div } 3 = 4$
 $r = 13 - 4 * 3 = 1$
 $y = x = 3$
 $x = r = 1$

$$= \text{gcd}(1, 3) =$$

$$\begin{aligned} 1 &= 109 * 197 - 61 * 352 \\ 1 &= 48 * 197 - 61 * 352 + 61 * 197 \\ 1 &= 48 * 197 - 61 * (352 - 1 * 197) \end{aligned}$$

$$\begin{aligned} 1 &= 48 * 197 - 61 * 155 \\ 1 &= 48 * (197 - 1 * 155) - 13 * 155 \end{aligned}$$

$$\begin{aligned} 1 &= 48 * 42 - 13 * 155 \\ 1 &= 9 * 42 - 13 * 155 + 39 * 42 \\ 1 &= 9 * 42 - 13 * (155 - 3 * 42) \end{aligned}$$

$$\begin{aligned} 1 &= 9 * 42 - 13 * 29 \\ 1 &= 9 * (42 - 1 * 29) - 4 * 29 \end{aligned}$$

$$\begin{aligned} 1 &= 9 * 13 - 4 * 29 \\ 1 &= 13 - 4 * 29 + 8 * 13 \\ 1 &= 13 - 4 * (29 - 2 * 13) \end{aligned}$$

$$1 = 13 - 4 * 3$$

Working from the bottom up:

$d = 3 \text{ div } 1 = 3$
 $r = 3 - 3 * 1 = 0$
 $y = x = 1$
 $x = r = 0$
 $= 1$

$\gcd(197, 352) = 1 = 109 * 197 - 61 * 352$ matching it with $\gcd(x, y) = s*x + t*y$

$s = 109, t = 61$

multiplicative inverse of $x \bmod y$ is $s \bmod y$.

Therefore, multiplicative inverse of $197 \bmod 352$ is $109 \bmod 352 = 109$